

Dropmore Infant School Written Calculation Policy



Addition

Children need to understand the concept of addition as:

•Combining two or more groups to give a total or sum.

•Increasing an amount

They also need to understand and work with certain principles:

Inverse of subtraction
It is commutative - 5 + 3 = 3 + 5

•It is associative -5 + 3 + 7 = 5 + (3+7)



Stage 1- Addition – countin	g altogether (EYFS)		
Teaching	Examples	Success criteria	Skill and knowledge
Children should count two sets of quantities and find how many altogether.		 Children point to each object as they count (touch count) 	 Understanding that a group changes quantity when something is added
Children are taught that addition is combining of two or more amounts.		Vocabulary	Resources
They begin by counting all of the items in the groups. Children are encouraged to think of a mental image of the size of numbers.	1 2 3 4 5 6	Add Plus More Greater quantity Addition Altogether Increasing	Counters Beads Counting objects Unifix cubes



Stage 2- Addition – countin	g on (EYFS/Y1)		
Teaching	Examples	Success criteria	Skill and knowledge
Children should count two sets by covering the larger amount. They should then count on the other amount. Children learn to think about addition as combining amounts in	Conter resources can be used to demonstrate counting on. Numicon is very helpful for children to recognise the value of the number.	 Start with the greatest number Count on Find the solution 	 Knowing the numerical value of a quantity e.g. recognising and identifying the '4' piece of numicon without touch counting the holes Being able to identify the largest quantity to begin with Understanding of symbols + and = Beginning to see and recognise patterns within numbers and groups of numbers
practical and real-life situations. They begin to record addition number sentences e.g. 4 + 2 = 6	5 6 5 6 Fluency facts - Number bonds to 10 and 20	Vocabulary Add Plus More Greater quantity Addition Altogether Increasing Count on What comes next?	Resources Counters Beads Counting objects Unifix cubes Numicon Base 10 cubes Cuisenaire



Stage 3 - Addition – using b	pase 10 to add a 2-digit number and ones (Y1)		
Teaching	Examples	Success criteria	Skill and knowledge
Children use base 10 equipment to support their developing understanding of addition Children should also start	11 + 5 =	 Start with the greatest number Split into tens and ones Count on Find the solution 	Counting forwards in ones • Counting using one to one correspondence • Being able to identify the largest quantity • Understanding place value of tens and ones • Understanding of symbols = and +
to draw their own representations of base 10 equipment using lines for tens and dots for ones.	11 cubes are lined up (1 ten and 1 unit/ one). 5 cubes are added to the line of 11 giving a total of 16. Fluency in partitioning numbers	Vocabulary Add Plus More Sum Addition Increasing Tens Ones Units Altogether Count on What comes next?	Resources Base 10 cubes (including interlinking 1cm cubes) Other resources may be used to support this but must reflect place value of tens and ones: Place value Counters Bead strings Unifix cubes Numicon Cuisenaire

Stage 4 - Addition – using b	base 10 to add a 2-digit number and tens (Y1/Y2)		
Teaching	Examples	Success criteria	Skill and knowledge
Children use base 10 equipment to support their developing understanding of addition	34 + 20	 Start with the greatest number Split into tens and ones Count on Find the solution 	Counting forwards in ones • Counting using one to one correspondence • Being able to identify the largest quantity • Understanding place value of tens and ones • Understanding of symbols = and +
		Vocabulary	Resources
Children should also start to draw their own representations of base 10 equipment using lines for tens and dots for ones.	Children should draw the diagrams of the equipment.	Add Plus More Sum Addition Increasing Tens Ones Units Altogether Count on What comes next?	Base 10 cubes (including interlinking 1cm cubes) Other resources may be used to support this but must reflect place value of tens and ones: Place value Counters Bead strings Unifix cubes Numicon Cuisenaire



Stage 5 - Addition – Using	Base 10 – 2-digit addition not crossing the bound	ary (Y2)	
Teaching	Examples	Success criteria	Skill and knowledge
Children continue to use base 10 equipment to support their calculations, with an increasing number of digits	34 + 23	 Draw/ collect equipment Count the ones first Count the tens Add the tens and ones together Find the solution 	Counting forwards in ones and tens • Understanding place value of tens and ones • Understanding which digit represents tens and which represents ones • Partition into tens and ones • Ones must be counted first (for the purposes of teaching
Children should be taught how to record their own drawing of base 10 equipment using lines for tens and dots for ones.	Children should draw the diagrams of the equipment.	Vocabulary Add Plus More Sum Addition Increasing Tens Ones Digit Partition Multiples Multiples of 10	exchanging) Resources Base 10 cubes (including interlinking 1cm cubes) Other resources may be used to support this but must reflect place value of tens and ones: Place value Counters Bead strings Unifix cubes Numicon Cuisenaire



Stage 6 - Addition – Using I	Base 10 – 2-digit addition crossing the boundary (\	(2)	
Teaching	Examples	Success criteria	Skill and knowledge
Children continue to use base 10 equipment to support their calculations, with an increasing number of digits and with crossing the tens boundary. Children will be taught to exchange up and change	Children should draw the diagrams of the equipment and show their exchange	 Draw/ collect equipment Count the ones first Exchange up the ones for ten if there are more than 10 ones. Count the tens Add the tens and ones together Find the solution 	 Counting forwards in ones and tens Understanding place value of tens and ones Understanding which digit represents tens and which represents ones Partition into tens and ones Ones must be counted first (for the purposes of teaching exchanging)
10 ones/ units for a ten piece. Once children have exchange they then follow the success criteria		Vocabulary Add Plus More Sum Addition Increasing Tens Ones Digit Partition Exchanging Crossing the boundary	Resources Base 10 cubes (including interlinking 1cm cubes) Other resources may be used to support this but must reflect place value of tens and ones: Place value Counters Bead strings Unifix cubes Numicon Cuisenaire



 Teaching	ing to use the column method (Y2/ Y3) Examples	Success criteria	Skill and knowledge
Children are applying prior learning of partitioning into writing the addition in the column method. Children will be taught to exchange up and change 10 ones/ units for a ten piece.	Not crossing the boundary $ \begin{array}{c cccc} \hline Tens & Ones \\ \hline \hline 0 & 0 & 0 \\ $	 Success criteria Draw/ collect equipment Count the ones first Exchange up the ones for ten if there are more than 10 ones. Count the tens Add the tens and ones together Find the solution 	 Counting forwards in ones and tens Understanding place value of tens and ones Understanding which digit represents tens and which represents ones Partition into tens and ones Ones must be counted first (for the purposes of teaching exchanging)
Once children have exchanged up they then follow the success criteria Children use place value grid to represent their numbers, they then exchange ten ones for a ten piece and move this to the correct column. They then follow the success criteria.	Exchanging/ crossing the boundary- $ \begin{array}{r} \hline \text{Tens} & \text{Ones} \\ $	Vocabulary Add Plus More Sum Addition Increasing Tens Ones Digit Partition Exchanging Crossing the boundary Column Place Value Carrying Over	Resources Base 10 cubes (including interlinking 1cm cubes) Other resources may be used to support this but must reflect place value of tens and ones: Place value Counters Bead strings Unifix cubes Numicon Cuisenaire



Subtraction

Children need to understand the concept of subtraction as: •Removal of an amount from a larger group (take away) •Comparison of two amounts (difference) They also need to understand and work with certain principles: •Inverse of addition •It is NOT commutative - 5 - 3 = 3 - 5 •It is NOT associative - (9-3)-2=9-(3-2)

Stage 1 - Subtraction – Tak	ing away (EYFS)		
Teaching	Examples	Success criteria	Skill and knowledge
Children will take the required amount of objects by taking one at a time. Children will the count how many objects are left. Children are encouraged to think of a mental image of the size of numbers.	l take the ount of objects ne at a time. I the count objects are left. e encouraged a mental image	 Children remove an object one at a time to the required amount Children point to each object as they count (touch count) 	Understanding that a group changes quantity when something is taken away • Encourage children to think of a mental image of the value of the number (quantity) • Knowing the numerical value of a quantity e.g. recognising and identifying the '4' piece of numicon without touch counting the holes
	12345	Vocabulary	Resources
		Subtract Take away Less Fewer Smaller quantity Subtraction How many left? Decreasing	Counters Beads Counting objects Unifix cubes

Stage 2 - Subtraction – cou	nting back (Y1)		
Teaching	Examples	Success criteria	Skill and knowledge
Children will develop this skill of taking away by counting back in sequence as they 'take away' an item. Children learn to think about subtraction as 'take	 8 7 6 9-4=5 	 Start with the greatest number Take away one item at a time Say out loud the number each time you count back. Vocabulary 	 Knowing the numerical value of a quantity e.g. recognising and identifying the '4' piece of numicon without touch counting the holes Being able to count backwards in ones
away' in practical and real-life situations. They begin to record number sentences. E.g. 9 – 4= 5	Numicon is a valuable resource that can be used to support counting back.	Subtract Take away Less Fewer Smaller quantity Subtraction How many left? Decreasing Count back What comes before?	Counters Beads Counting objects Unifix cubes

Stage 3 - Subtraction – Ba	se 10 and Number lines/ tracks (Y1)		
Teaching	Examples	Success criteria	Skill and knowledge
Children use base 10 equipment alongside a number track to develop their understanding of subtraction. Number tracks are	3 - 4 = ? 1 2 3 4 5 6 7 8 9 10 2 3 9 10 2	 Start with the greatest number Take away one item at a time Say out loud the number each time you count back. 	 Counting backwards in ones Partition numbers in different ways e.g. 5 could be partitioned as 3 and 2 or 1 and 4 Know and quickly derive number bonds up to and including 10
preferable to number lines as they give children parameters to place their objects within.	 2 3 4 5 6 7 8 9 10111213 1. 13 cubes are lined up 2. 4 cubes are removed from the end of the line. Children are encouraged to count back through the sequence of numbers each time they remove one cube. 3. The number track supports learning as the children can use this check they have counted back to the correct number. 	Vocabulary Subtract Take away Less Fewer Smaller quantity Subtraction How many left? Decreasing Count back What comes before? Partition Number facts Subtraction facts What do you know? Tens Ones	Resources Base 10 Number tracks Number lines Other place value objects may be used alongside the main resources.

	e 10 with a 2-digit number and subtracting ones (
Teaching	Examples	Success criteria	Skill and knowledge
Children use base 10 to represent 2-digit numbers and to subtract them from their first number. Children are taught to draw the base ten using a	No exchange down: 27 - 5 = ?	 Start with the greatest number Exchange down a ten if needed Subtract ones Subtract tens 	 Counting backwards in ones Partitioning numbers into 10s and 1s Starting quantity is plotted at the end of a number line
line for a ten and a dot for		Vocabulary	Resources
a one. Subtraction becomes more difficult for children when crossing the boundary when exchanging is needed. When a number contains multiple tens children find it confusing to suggest subtracting ones. Where there is a greater amount of ones that needs to be subtracted a ten should be exchanged down for 10 ones.	Exchange down: eq. 21 - 5 f = 1 ten and 6 ones = 16	Subtract Take away Less Fewer Smaller quantity Subtraction How many left? Decreasing Count back What comes before? Partition Number facts Subtraction facts What do you know? Tens Ones	Base 10 Number tracks Number lines Other place value objects may be used alongside the main resources.

Teaching	Examples	Success criteria	Skill and knowledge
I eaching Children use base 10 to represent 2-digit numbers and to subtract them from the first number. Children are taught to draw the base ten using a line for a ten and a dot for a one.	o exchange down: 54 - 23 = ?	 Start with the greatest number Count the ones to see if exchanging is needed Exchange down a ten if needed Subtract ones Subtract tens 	 Counting backwards in tens Understanding of place value of tens and ones Starting quantity is plotted at the end of a number line
It is highly encouraged for children to use jottings and diagrams to support them. Subtraction becomes more difficult for children when crossing the boundary when exchanging is needed. This is explained in stage 6.	= 3 tens and 1 one = 31	Vocabulary Subtract Take away Less Fewer Smaller quantity Subtraction How many left? Decreasing Count back What comes before? Partition Number facts Subtraction facts What do you know? Tens Ones Jumps of 10 Multiples Multiples of 10	Resources Base 10 Number tracks Number lines Other place value objects may be used alongside the main resources.

Stage 6 - Subtraction – Sub	tracting using Base 10 with two 2-digit num	ıbers (Y2)	
Teaching	Examples	Success criteria	Skill and knowledge
Children use base 10 to represent 2-digit numbers and to subtract them from the first number. Children are taught to draw the base ten using a line for a ten and a dot for a one.	Exchange down: 54 - 28	 Start with the greatest number Count the ones to see if exchanging is needed Exchange down a ten if needed Subtract ones Subtract tens 	 Starting quantity is plotted at the end of a number line Counting forwards and backwards in jumps of tens and ones
It is highly encouraged for children to use jottings and diagrams to support them. Subtraction becomes more difficult for children when crossing the boundary when exchanging is needed. Children are taught to draw/collect equipment of only the first number. Then to count the ones to check if they need to exchange. The exchange of a ten piece to ten ones takes place. Then children carry on the rest of the success criteria.	= 2 tens and 6 ones = 26	Vocabulary Subtract Take away Less Fewer Smaller quantity Subtraction How many left? Decreasing Count back What comes before? Partition Number facts Subtraction facts What do you know? Tens Ones Jumps of 10 Multiples Multiples of 10	Resources Base 10 Number tracks Number lines Other place value objects may be used alongside the main resources.

Success criteria	Skill and knowledge
 Start with the greatest number Count the ones to see if exchanging is needed Exchange down a ten if needed Subtract ones Subtract tens Vocabulary 	 Counting forwards in ones and tens Understanding place value of tens and ones Understanding which digit represents tens and which represents ones Partition into tens and ones Ones must be counted first (for the purposes of teaching exchanging) Resources
Subtract Take away Less Fewer Smaller quantity Subtraction How many left? Decreasing Count back What comes before? Partition Number facts Subtraction facts What do you know? Tens Ones Jumps of 10 Multiples Multiples of 10 column row	Base 10 Number tracks Number lines Other place value objects may be used alongside the main resources.

Stage 7 - Subtraction - Colu			
Teaching	Examples	Success criteria	Skill and knowledge
Children are applying prior learning of partitioning into writing the subtraction in the column method. Children will be taught to exchange down and change 1 ten for ten ones.	No exchange down: Tens Ones $T \bigcirc 45$ -12 -12 -3 Exchange down: Tens Ones $T \bigcirc 45$ -27	 Start with the greatest number Count the ones to see if exchanging is needed Exchange down a ten if needed Subtract ones Subtract tens Vocabulary Subtract Take away Less Fewer 	 Counting forwards in ones and tens Understanding place value of tens and ones Understanding which digit represents tens and which represents ones Partition into tens and ones Ones must be counted first (for the purposes of teaching exchanging) Resources Base 10
Once children have exchanged up they then follow the success criteria Children use place value grid to represent their numbers, they then exchange 1 ten for ten ones and move these to the correct column. They then follow the success criteria.	TensOnesTO $3/4$ $1/5$ -2 7TensOnes $\frac{T}{3/4}$ $1/5$ -2 7 $\frac{T}{3/4}$ $1/5$ -2 7 $\frac{T}{3/4}$ $1/5$ -2 7 $\frac{T}{8}$ TensOnes $\frac{T}{3/4}$ $\frac{Tens}{8}$ $\frac{T}{8}$ $\frac{Tens}{8}$ $\frac{1}{3/4}$ $\frac{1}{8}$ $\frac{1}{8}$	Smaller quantity Subtraction How many left? Decreasing Count back What comes before? Partition Number facts Subtraction facts What do you know? Tens Ones Jumps of 10 Multiples Multiples of 10 column row	



Multiplication

Children need to understand the concept of multiplication as:

•Repeated addition

•Can be represented as an array

They also need to understand and work with certain principles:

•It is the inverse of division

•It is commutative

•It is associative



Stage 1 - Multiplication - Doubling (EYFS)			
Teaching	Examples	Success criteria	Skill and knowledge
Children begin learning about the concept of	The butterfly has the same number of spots on both sides of the wings.	Touch counting where needed.	• Understanding the meaning of the language 'same' •
multiplication through doubling.			Understanding basic equivalence
These will be practical, real	\frown		
life situations.	$(\bullet \land \bullet)$		
		Vocabulary	Resources
Children are encouraged to develop a mental image of the size of numbers. They can begin to record		Double Same Equal	Butterfly/ ladybird templates Numicon Counters
these situations using	3 spots on one side and 3 spots on the other		
pictures and diagrams.	side.		
	3+3 = 6 or double 3 is 6		
	Numicon can be used on the wings to		
	demonstrate doubles.		



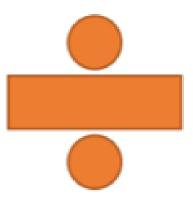
Stage 2 - Multiplication - Re	epeated addition (Y1)			
Teaching	Examples		Success criteria	Skill and knowledge
Repeated addition follows on from doubling but uses	2 + 2 + 2 = 1		•	 Understanding of counting in 2's, 5's and 10's Understanding equal groups of
a wider vocabulary.	2 4	6		2, 5 and 10
	Numicon can also be used to re	present groups of		
	numbers.		Vocabulary	Resources
Children should be			Double Same Equal Repeat Lots of	Counters Numicon
encouraged to use the language of multiplication to enable them to correctly write multiplication number sentences				Counting objects



Stage 3 - Multiplication - Ar	Stage 3 - Multiplication - Arrays (Y2)				
Teaching	Examples	Success criteria	Skill and knowledge		
Children use arrays to enable them to visualise the multiplication.	E,q, $3 \propto 4$		 Understanding the difference between a row and a column Understanding of the x symbol 		
Rows represent the number of groups. Columns represent the number in each group.		Vocabulary Array Times Lots of Groups of Row Column Repeat Representation Multiply	Resources		
It is important that children understand the x symbol represented lots of but us spoken as times or multiplied.					



Stage 4 - Multiplico	Stage 4 - Multiplication - Arrays using known facts(Y2)				
Teaching	Examples	Success criteria	Skill and knowledge		
	00000000	•	• Double any multiple of 10 up to 100 • Understanding that doubling is adding any		
	00000000		number to itself • Understanding that doubling is multiplying by 2 • Recall multiplication tables		
		Vocabulary	Resources		
	0 10 20 30	Array Times Lots of Groups of Multiply Row Column Facts Repeat Product Multiple Factor			



Division

Children need to understand the concept of division as:

•Repeated subtraction

They also need to understand and work with certain principles:

•It is the inverse of multiplication

 $\bullet It$ is NOT commutative

 $\bullet It$ is NOT associative



Stage 1 – Division - halving (EYFS)				
Teaching	Examples	Success criteria	Skill and knowledge	
Children should experience practical calculation opportunities involving equal groups and equal sharing.	A lady bird has 6 sports on its back. Can you share them equally between both sides?	•	 Understanding that halving is sharing into 2 groups equally. Understanding of equivalence Understanding that halving is splitting down the middle into 2 	
		Vocabulary Half Equal Same Split	Resources	



Stage 2 – Division – division as sharing (Y1/Y2)				
Teaching	Examples	Success criteria	Skill and knowledge	
Children start their learning of division by	12 divided by 2	•	• Understanding the language and symbol for	
sharing.	12 gems are shared equally between 2 people. How many gems to they each get?		division • Know multiples of 2 5 and 10 • Understand and apply related division facts e.g. 8 divided by 2 =	
Children may use the 'one	00000000000		4 so 80 divided by 2 = 40	
for you and one for me'		Vocabulary	Resources	
strategy until all the items have been given out. This		Equal Share Divide Divided by		
strategy ensures sharing into equal groups.	15 gems shared equally between 3 people.			
	They get 5 💮 each.			



Stage 3 – Division – divisior	ι as grouping (Y1/Y2)		
Teaching	Examples	Success criteria	Skill and knowledge
To develop more efficient strategies for division, children need to develop the understanding of division as grouping.	This can be through grouping images into equal groups.	•	 Understanding the language and symbol for division Know multiples of 2,5 and 10 Understand and apply related division facts e.g. 8 divided by 2 = 4 so 80 divided by 2 = 40
		Vocabulary	Resources
	$12 \div 4 = 3$ $12 \div 6 = 2$ $12 \div 2 = 6$	Equal groups Groups of Divide Divided by	Numicon Counting objects Unifix Bead strings Counters Connecting cubes



Stage 4 – Division – division as grouping using jottings (Y1/Y2)				
Teaching	Examples	Success criteria	Skill and knowledge	
Children will begin to investigate ways to represent division calculations. The could use bar models, number lines or sharing	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	•	 Know multiples of 2,5, 10 and 3 • Understand and apply related division facts e.g. 8 divided by 2 = 4 so 80 divided by 2 = 40 	
circles to calculate their	There are 4 groups now.	Vocabulary	Resources	
division. They many also use arrays to show the commutative representation between multiplication and division		Equal groups Groups of Divide Divided by Multiples	Numicon Counting objects Unifix Bead strings Counters Connecting cubes	



Stage 5 – Division – division as grouping with remainders (Y2/ Y3)				
Teaching	Examples	Success criteria	Skill and knowledge	
Children need to understand that division calculations sometimes have remainders. Depending on the question children may either need to leave the remainder as how many are left over or	E.g. 13 divided by 3 =? There are four groups of 3 with one left over 13 divided by 3 = 4 r 1	• Vocabulary Equal groups Groups of Divide	 Know multiples of 2,5, 10 and 3 • Understand and apply related division facts e.g. 8 divided by 2 = 4 so 80 divided by 2 = 40 • Understanding quantities cannot always be split into equal groups with nothing left over Resources Numicon 	
may have to round up or down.	Round DOWN: I have 13p. sweets are 3p each. How many can I buy? Remaining 1p is not enough to by another sweet Round up: Apples are packed into boxes of 3. There are 13 apples how many boxes do I need? 1 remaining apple still needs to be in a box	Divided by Multiples Remainder Left Over	Counting objects Unifix Bead strings Counters Connecting cubes	